Alg 3 Summer Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

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 WS Assessment

 Target 8:

APPLICATION OF Exponential and LOGARITHM functions

**I can:**

* Apply exponential and logarithmic functions to solve problems.
* **Unit 3: Logarithms & Exponentials**
* **C**[**CSS.MATH.CONTENT.HSF.LE.A.4**](http://www.corestandards.org/Math/Content/HSF/LE/A/4/): For exponential models, express as a logarithm the solution to *abct* = *d* where *a*, *c*, and *d*are
* [**CCSS.MATH.CONTENT.HSF.IF.C.8.B**](http://www.corestandards.org/Math/Content/HSF/IF/C/8/b/): Use the properties of exponents to interpret expressions for exponential functions. For example, identify percent rate of change in functions such as y = (1.02)ᵗ, y = (0.97)ᵗ, y = (1.01)12ᵗ, y = (1.2)ᵗ/10, and classify them as representing exponential growth or decay.
* [**CCSS.MATH.CONTENT.HSF.BF.A.1**](http://www.corestandards.org/Math/Content/HSF/BF/A/1/): Write a function that describes a relationship between two quantities.\*
* [**CCSS.MATH.CONTENT.HSF.BF.A.1.A**](http://www.corestandards.org/Math/Content/HSF/BF/A/1/a/): Determine an explicit expression, a recursive process, or steps for calculation from a context.
* [**CCSS.MATH.CONTENT.HSF.BF.A.1.B**](http://www.corestandards.org/Math/Content/HSF/BF/A/1/b/): Combine standard function types using arithmetic operations. *For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model*.
* [**CCSS.MATH.CONTENT.HSA.SSE.A.1.B**](http://www.corestandards.org/Math/Content/HSA/SSE/A/1/b/): Interpret complicated expressions by viewing one or more of their parts as a single entity. *For example, interpret P(1+r)n as the product of P and a factor not depending on P*.

**Interest Rate Problems** $A=P(1+\frac{r}{n})^{nt}$ Continuously A = Pert

A $1,000 deposit is made at a bank that pays 12% compounded annually. How much will you have in your account at the end of 10 years? What if it is compound monthly? weekly?

An $1,000 investment is made in a trust fund at an annual percentage rate of 12%, compounded monthly. How long will it take the investment to reach $2,000?

If you invested $1,000 in an account paying an annual percentage rate (quoted rate) compounded daily (based on a bank year of 360 days) and you wanted to have $2,500 in your account at the end of your investment time, what interest rate would you need if the investment time were 1 year, 10 years, 20 years, 100 years?

If you invested $1,000 in an account paying an annual percentage rate (quoted rate) of 12%, compounded continuously, how much would you have in you account at the end of 1 year, 10 years, 20 years, 100 years?

*Now you do.* If you invested $1,000 in an account paying an annual percentage rate (quoted rate) of 12%, compounded weekly, how much would you have in your account at the end of 1 year, 10 years, 20 years, 100 years? How long will it take the investment to reach $2,000? What if you want to have $2000 in 1 year, then what would be the interest rate ?

**Mortgage Problems** $P=\frac{rM}{1-(1+\frac{r}{n})^{-nt}}÷n$

 where P = the payment, r = the annual rate, M = the mortgage amount (loan),

t = the number of years, and n = the number of payments per year (most of time, monthly)

What is the monthly payment on a mortgage of $75,000 with an 8% interest rate that runs for 20 years, 25 years, 30 years? How much interest is paid over 20 years, 25 years, 30 years?

TI 84 – Stamp

Now you do and check with TI 84

Find the monthly payments on a $100000, 30-year mortgage, with monthly payments at 9.5%. How much interest will you have over the 30 years?

**Population Problems**

Suppose that you are observing the behavior of cell duplication in a lab. In one experiment, you started with one cell and the cells doubled every minute. Write an equation with base 2 to determine the number (population) of cells after one hour.

Determine how long it would take the population (number of cells) to reach 100,000 cells.

Write an equation with base 5 that is equivalent to the equation *f* (*t*) = 2t.

Now you do

Suppose that you are observing the behavior of cell duplication in a lab. In one experiment, you started with one cell and the cells tripling every minute. Write an equation with base 3 to determine the number (population) of cells after one hour.

Determine how long it would take the population (number of cells) to reach 100,000 cells.

Write an equation with base 10 that is equivalent to the equation *f* (*t*) = 3t.

Radioactive Decay Problems $f\left(t\right)=ae^{bt}$ b is called the decay constant

If you start a biology experiment with 5,000,000 cells and 45% of the cells are dying every minute, how long will it take to have less than 1,000 cells?

Now you do

Hospitals utilize the radioactive substance iodine-131 in the diagnosis of conditions of the thyroid gland. The half-life of iodine-131 is eight days. Determine the decay constant b. If a hospital acquires 2 g of iodine-131, how much of this sample will remain after 20 days ? How long will it be until only 0.01 g remains?

Earthquake Problems Charles Richter scale $M=log\frac{I}{S}$

I is the intensity of the earthquake; S is the intensity of standard (A = 10-4 cm)

Early in the 20th century the earthquake in San Francisco registered 8.3 on the Richter scale. In the same year, another earthquake was recorded in South America that was four time stronger. What was the magnitude of the earthquake in South American?

A recent earthquake in San Francisco measured 7.1 on the Richter scale. How many times more intense was the San Francisco earthquake described above at the begin of the century.

Now you do

Early in the century an earthquake measured 8.0 on the Richter scale. In the same year, another earthquake was recorded that measured six time stronger on the Richter scale. What was the magnitude of the earthquake of the stronger earthquake?

**Assessment Target 8**

**I can…** exponents and logarithms in real life application

Let’s say your family plan to buy a new house. After doing some research from the housing market <https://www.zillow.com/portland-or/> you have found a house on sale at the price of

$\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_. With your good credit history, your bank agree to lend you this above loan at \_\_\_\_\_\_\_\_\_\_\_% <https://www.bankrate.com/oregon/mortgage-rates.aspx>

What is your monthly payment if you plan to pay off the loan in 30 years, 15 years. Show work

 (you can check your work with TI apps)

Now with the payment above in 30 years. Let say you will help in your parent $500 a month (add it into the payment), then how long it take to pay off the loan? How about just $100 a month? Show work